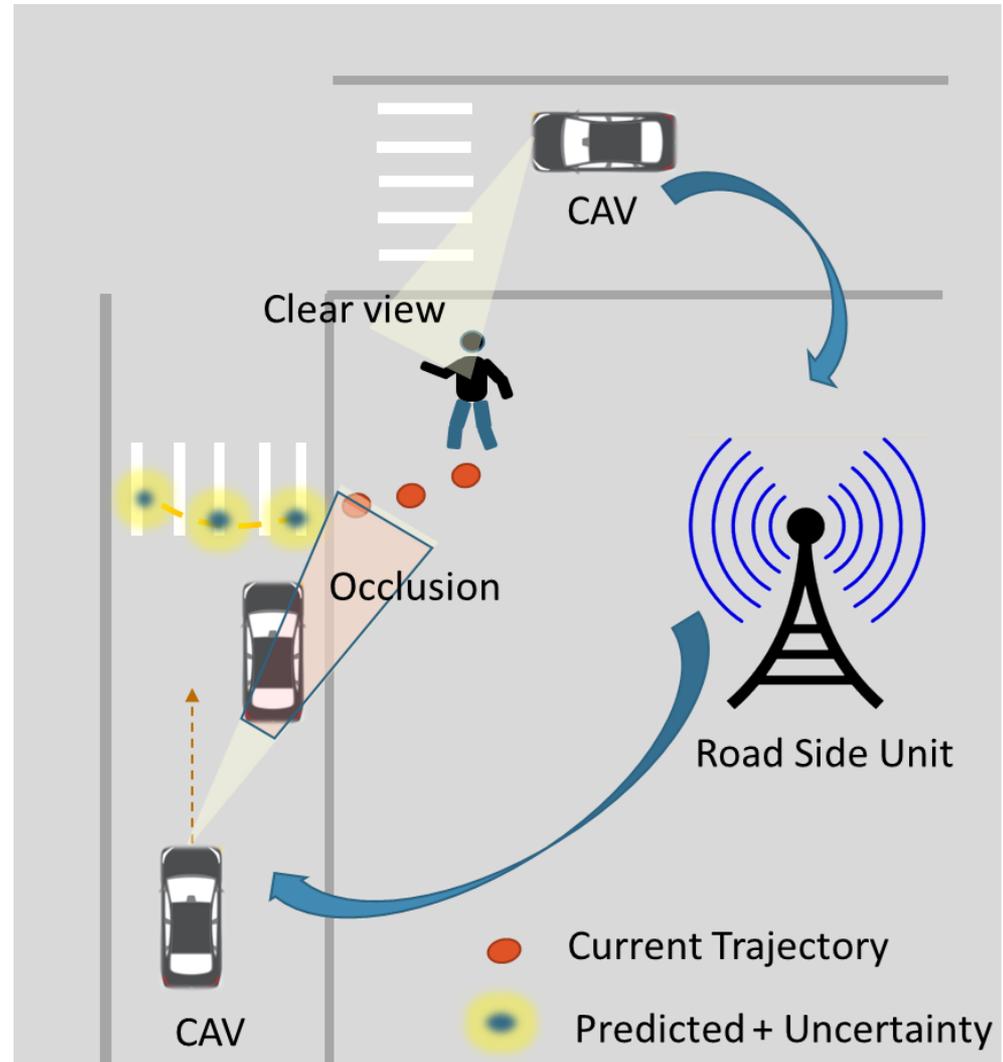


# Cooperative Prediction of Vulnerable Road Users (VRUs)

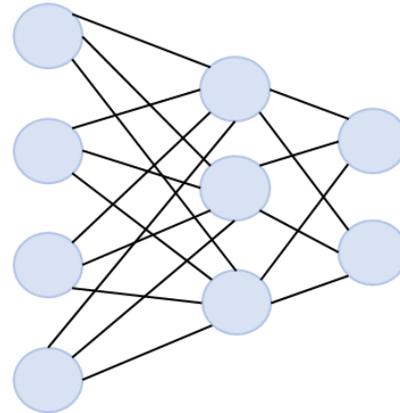
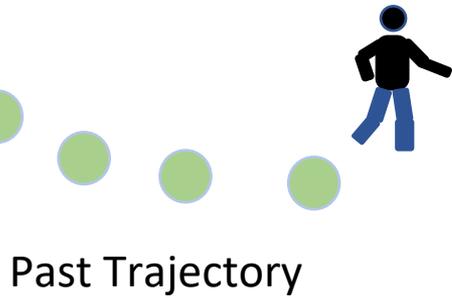
# Cooperative Prediction of Vulnerable Road Users (VRUs)

**Goal: Uncertainty estimation of future pedestrian trajectory using Probabilistic method**

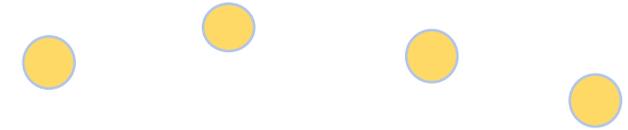
- Future state estimation due to occlusion is often difficult.
- Deterministic state prediction lacks robustness.
- VRU state information transferred via V2V or V2I communication.
- Ego CAV vehicle predicts future trajectory with uncertainty based on information.



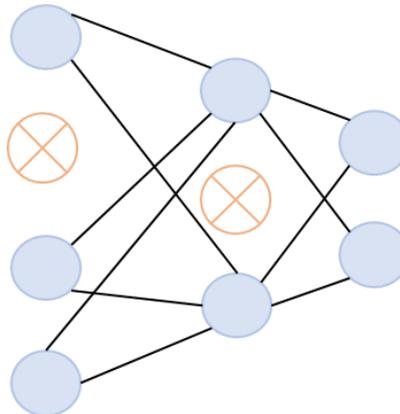
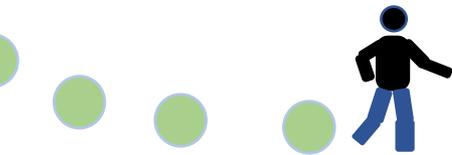
# Method: Probabilistic Prediction with weight dropout



Neural Network (NN)  
without Dropout



Deterministic Prediction  
gives point estimates (x,y)



NN with Monte Carlo  
Dropout of weights



Stochastic Prediction  
+  
Uncertainty (95% Confidence Interval)

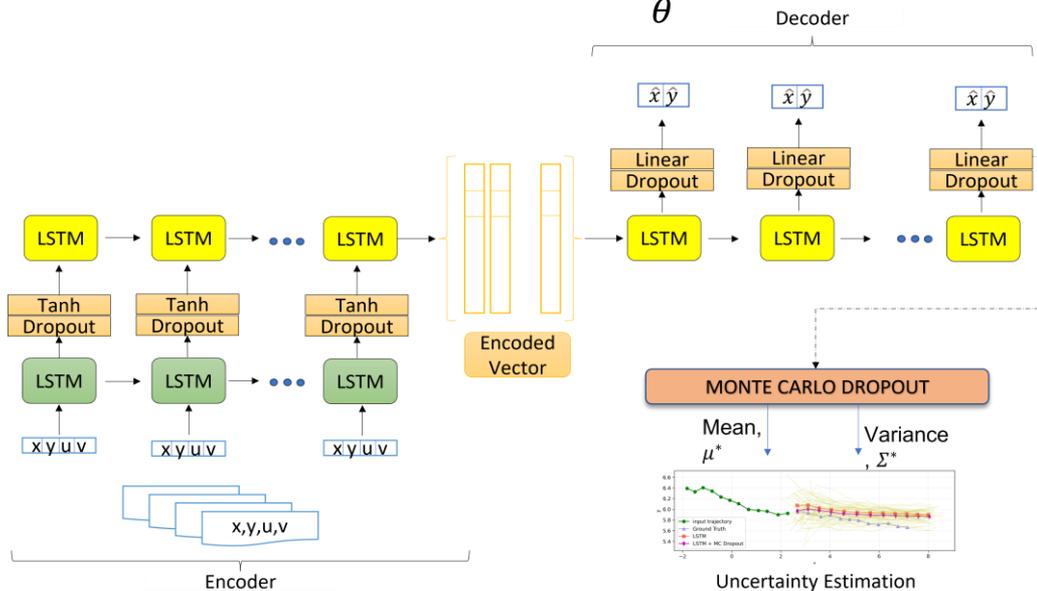
# Architecture: Neural Network models for Bayesian Inference

- Compared three neural network models; LSTM, 1D-CNN and CNN-LSTM for both deterministic as well as probabilistic prediction using MC dropout of weights.
- Prediction of future state (deterministic)/states (probabilistic),  $y^*$  based on test sample,  $x^*$  :

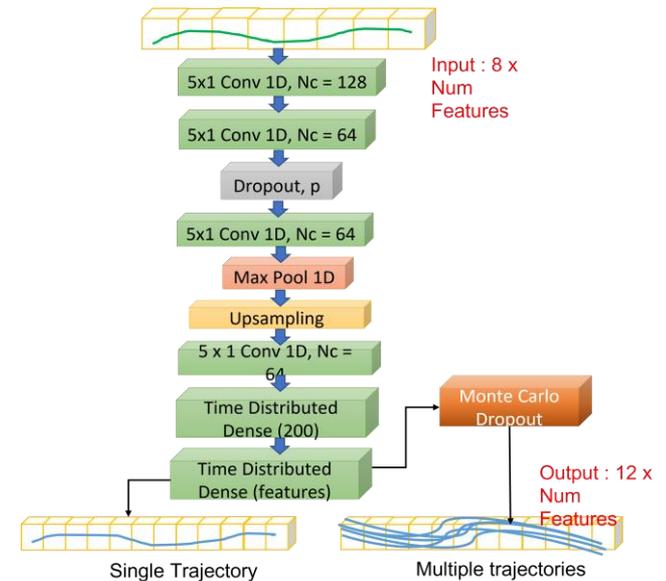
Training : Bayes Rule, 
$$P(\theta|X, Y) = \frac{P(X, Y|\theta)P(\theta)}{P(X, Y)}$$

Testing : 
$$p(y^*|x^*, X, Y) = \int_{\theta} p(y^*|x^*, \theta')p(\theta'|X, Y) d\theta'$$

$X, Y$  : Train Data,  
 $\theta$  : weights



(a) Long Short-Term Memory (LSTM)



(b) Convolutional Neural Network (CNN)

# Results: Probabilistic Prediction outperforms deterministic output



Performance metrics:

- a) Average Displacement Error (ADE):  
Mean of Euclidean distance between predicted and ground truth points.
- b) Final Displacement Error (FDE):  
Euclidean distance between the final point of estimated and ground truth trajectory

- Tested on two publicly available pedestrian datasets with five scenes.  
ETH dataset: ETH and Hotel scene  
UNIVERSITY dataset: ZARA1, ZARA2 UNIV
- Mean predicted path of probabilistic models was closer to ground truth with lower average ADE/FDE compared to deterministic prediction.

**Lower ADE/ FDE is better**

	ETH	HOTEL	ZARA1	ZARA2	UNIV	AVERAGE
S-LSTM [12]	1.09/2.35	0.79/1.76	0.47/1.00	0.56/1.17	0.67/1.40	0.72/1.54
SGAN [32]	0.87/1.62	0.67/1.37	0.35/0.68	0.42/0.84	0.76/1.52	0.61/1.21
Sophie [33]	0.70/1.43	0.76/1.67	0.30/0.63	0.38/0.78	0.54/1.24	0.54/1.15
Social-BiGAT [34]	0.69/1.29	0.49/1.01	<b>0.30/0.62</b>	<b>0.36/0.75</b>	0.55/1.32	0.48/1.00

Deterministic	<ul style="list-style-type: none"> <li>LSTM</li> <li>1D CNN</li> <li>CNN-LSTM</li> </ul>	LSTM	0.54/0.94	0.33/0.46	0.51/0.96	0.53/0.96	0.75/0.93	0.53/0.85
		1D CNN	0.71/0.90	0.71/1.04	0.75/1.02	0.86/1.16	0.95/1.24	0.79/1.07
		CNN-LSTM	0.68/1.11	0.98/1.29	0.73/0.99	0.95/1.27	0.87/1.11	0.84/1.15
Probabilistic	<ul style="list-style-type: none"> <li>LSTM + MC</li> <li>1D CNN + MC</li> <li>CNN-LSTM + MC</li> </ul>	LSTM + MC	0.55/0.94	<b>0.32/0.45</b>	0.51/0.96	0.54/0.96	0.59/0.84	<b>0.50/0.83</b>
		1D CNN + MC	0.69/0.84	0.58/0.79	0.73/0.99	0.85/1.15	0.71/0.85	0.71/0.92
		CNN-LSTM + MC	<b>0.48/0.82</b>	<b>0.3/0.48</b>	0.50/0.83	0.77/1.12	<b>0.53/0.86</b>	<b>0.51/0.82</b>

# Ablation Study: Effect of Dropout Probability and Long-term prediction horizon

## I. Dropout Probability ( $p$ )

- Stochastic dropout of weights with probability  $p$ .
- For  $p = 0.2, 0.3, 0.4, 0.5$ .  $p = 0.3$  implies 30% of weights are randomly dropped during each test inference.

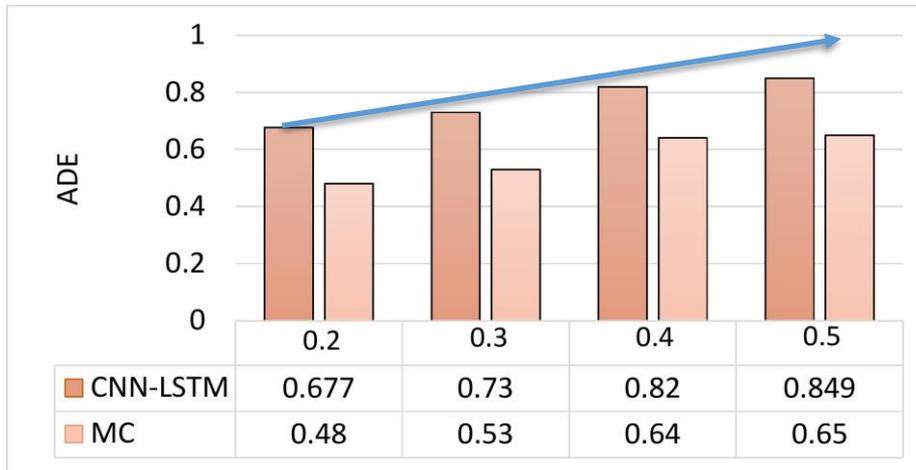


Fig. ADE with dropout probability,  $p$  for CNN-LSTM

- ADE increased with dropout probability,  $p$ .
- Mean of probabilistic prediction (MC) has lower ADE compared to deterministic (CNN-LSTM).

## II. Time Horizon ( $T_f$ )

- Quantify uncertainty in states for long term forecast.
- Considered future prediction horizon,  $T_f = 3.2, 4.8, 6.4, 8$  secs

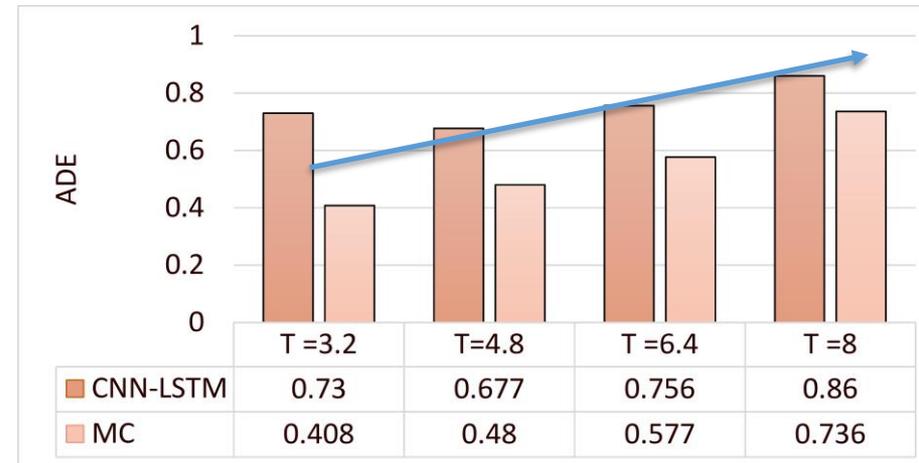


Fig. ADE with time horizon,  $T_f$  for CNN-LSTM

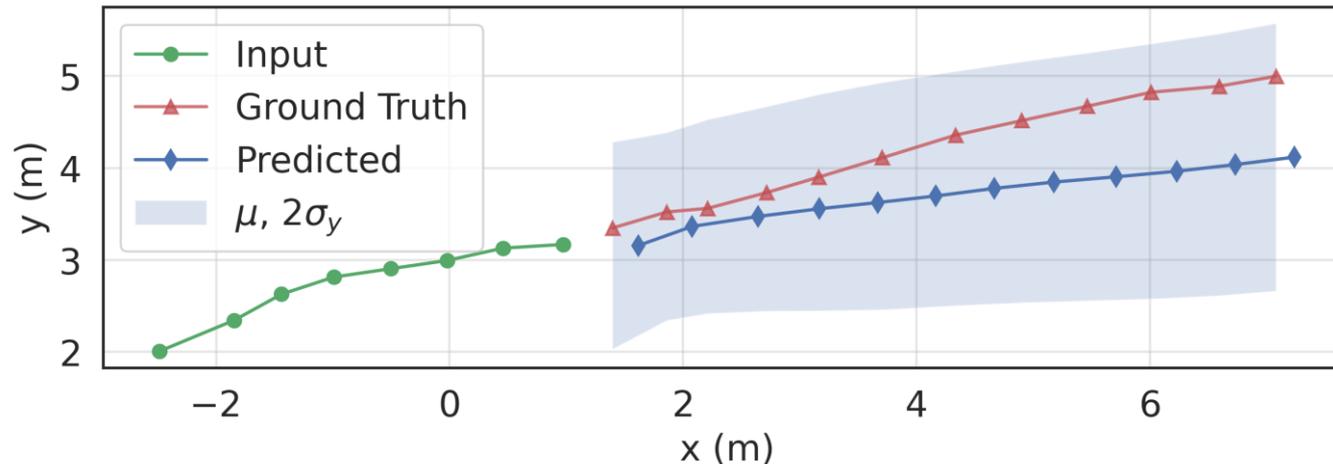
- ADE increased with Prediction horizon,  $T_f$ .
- It shows uncertainty grows with time.
- Mean of probabilistic prediction (MC) has lower ADE.

## Results: Estimated Trajectory with confidence Interval

- Neural Network is called N times where weights are dropped with probability, p for each pass generating a distribution of N predicted trajectories with:
- Based on 95% Confidence interval, 80% of test trajectories contain the ground truth.
- In future, perception/state uncertainty will be used for uncertainty propagation .

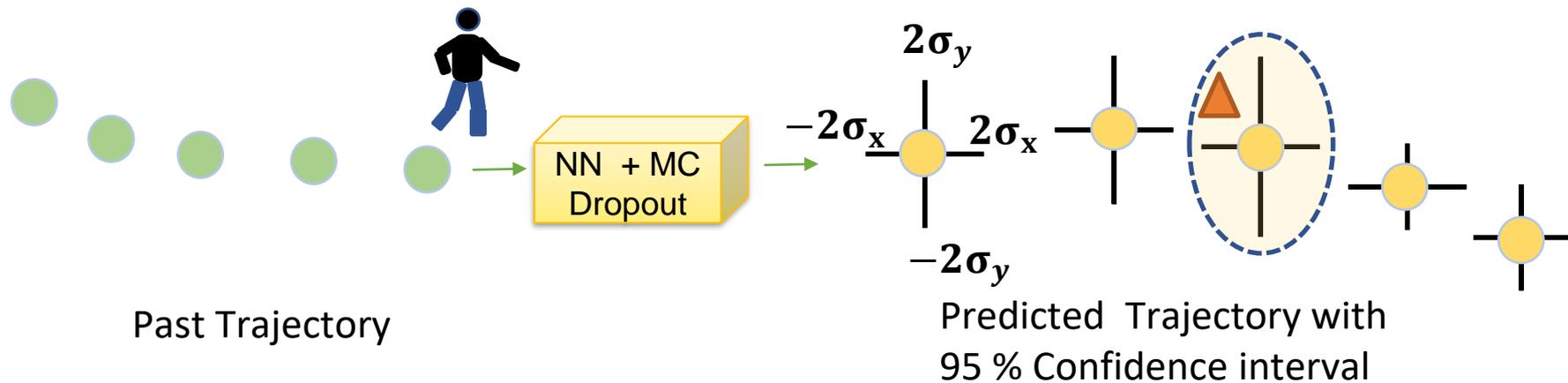
Mean,  $\bar{y} = \frac{1}{N} \sum_{n=1}^N y^*(n)$

Variance,  $\Sigma_{y^*} = \frac{1}{N} \sum_{n=1}^N (y^*(n) - \bar{y})^2$

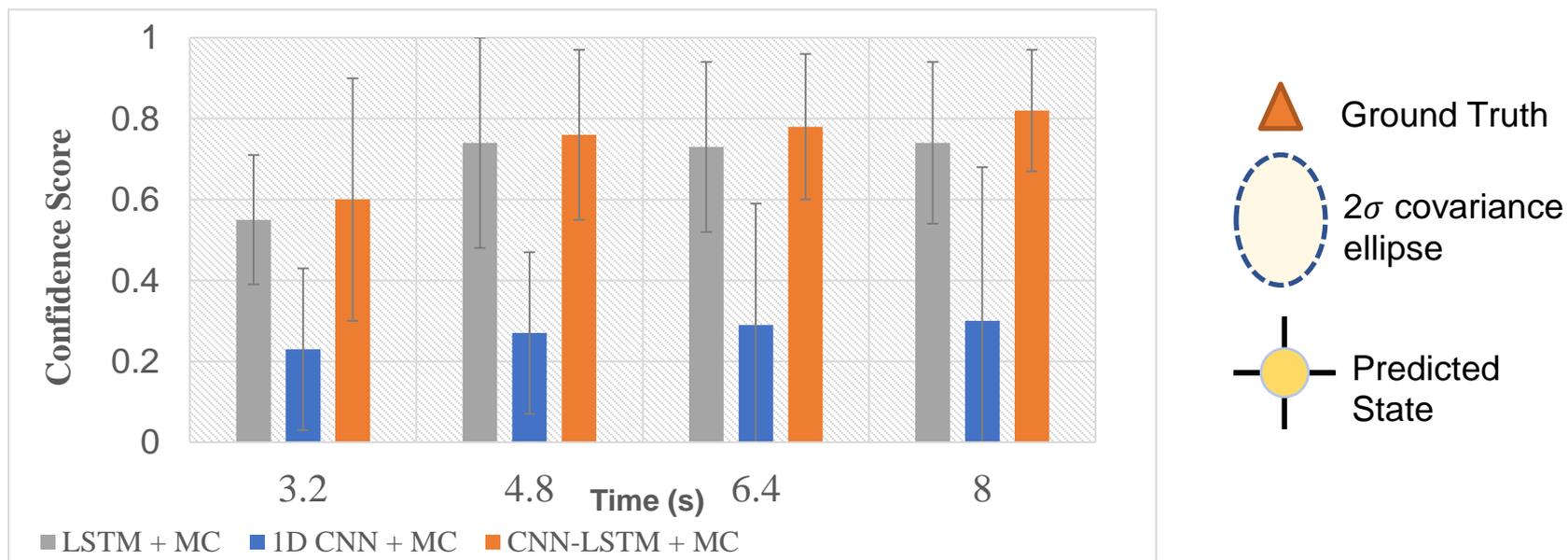


A. Nayak, A. Eskandarian and Z. Doerzaph, "Uncertainty Estimation of Pedestrian Future Trajectory Using Bayesian Approximation," in *IEEE Open Journal of Intelligent Transportation Systems*, vol. 3, pp. 617-630, 2022, doi: 10.1109/OJITS.2022.3205504.

# Results: Confidence Score



**Confidence Score: Whether the ground truth lies within 95% of predicted confidence interval**



Plot shows percentage of Ground truth lying within  $2\sigma$  covariance ellipse for ETH dataset.